# Bloat Control in Genetic Programming with a Histogram-based Accept-Reject Method

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## ABSTRACT

Recent bloat control methods such as dynamic depth limit (DynLimit) and Dynamic Operator Equalization (DynOpEq) aim at modifying the tree size distribution in a population of genetic programs. Although they are quite efficient for that purpose, these techniques have the disadvantage of evaluating the fitness of many bloated Genetic Programming (GP) trees, and then rejecting most of them, leading to an important waste of computational resources. We are proposing a method that makes a histogram-based model of current GP tree size distribution, and uses the so-called accept-reject method for generating a population with the desired target size distribution, in order to make a stochastic control of bloat in the course of the evolution. Experimental results show that the method is able to control bloat as well as other state-of-the-art methods, with minimal additionnal computational efforts compared to standard tree-based GP.

## **Categories and Subject Descriptors**

I.2.8 [Artificial Intelligence]: Problem Solving, Control Methods, and Search—*Heuristic methods*; G.3 [Probability and Statistics]: Probabilistic algorithms (including Monte Carlo)

# Keywords

Genetic Programming, Bloat Control, Acceptance Sampling

#### **General Terms**

Performance

The Histogram-based Accept-Reject Method for Genetic Programming (HARM-GP) is inspired from distributionbased bloat control techniques such as DynOpEq [4], but takes a different approach for defining the target distribution and evaluating fitnesses. Indeed, the target distribution with HARM-GP is defined from the size distribution of individuals at the previous generation, with a cut-off point determined from the best-so-far individual size, for reducing the frequency of large bloated individuals in the population. The cut-off point is evaluated at each generation as being half-way the current size of the best-so-far individual and the cut-off value of the previous generation. The target distribution ( $w_i$ ) at the right of the cut-off point is given by an

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exponential decay function parameterized by a  $\tau$  parameter corresponding to the size increase  $(x_i = x_0 + \tau)$  with half the frequency of the cut-off  $(w_0)$ :

$$w_i = w_0 \exp\left[-\ln(2) \cdot \frac{x_i - x_0}{\tau}\right].$$
 (1)

Moreover, the histogram of the source distribution is obtained with kernel density estimation, using a triangular kernel. Figure 1 presents an example of a source (boxes) and target histograms (shaded area) obtained with this method.

In HARM-GP, a new population is produced by the classical accept-reject method, a well-known Monte Carlo approach commonly used for generating random numbers for arbitrary distributions [2]. An accept probability is computed for each individual using the ratio between the target and source distribution values for the size of the individuals. Individuals are generated by crossover, mutation, and reproduction from the previous population and are tested for acceptation with this probability until the requested population size is obtained, without evaluating the candidates fitness. Therefore, in opposition to DynLimit [3] and DynOpEq, HARM-GP induces no supplementary fitness evaluations compared to standard GP.

Experiments are made over six bloat control approaches: **NoLimit**: standard GP without any bloat control;

**DepthLimit**: static depth limit [1] of 17;

DynLimit: dynamic depth limit [3], with initial limit of 6;

**DynOpEq**: with bin width of 5 [4], except for Symbolic Regression where a bin width of 1 is used;

**HARM5**: HARM-GP with a small half-life of  $\tau = 5$ , for strong bloat control;

**HARM40**: HARM-GP with a larger half-life of  $\tau = 40$ , leading to softer bloat control.

Experiments were performed using  $DEAP^1$  on runs with population size of 1000 individuals, crossover probability of 0.8, subtree mutation probability of 0.1 on the Symbolic Regression, Artificial Ant, and Parity-6 problems [1]. Tournament selection with 5 participants is used for the Symbolic Regression and Parity-6 problems, with runs stopped after a budget of 80k fitness evaluations. For the Artificial Ant, 100k evaluations are conducted, with 7 participants to tournaments. Figure 2 plots three graphs for the Artificial Ant problem. Table 1 presents a set of detailed measurements carried out on all three problems tested with the six bloat methods we compared. Results show that HARM-GP is able

<sup>&</sup>lt;sup>1</sup>Freely available at http://deap.googlecode.com.

Table 1: Experimental results. Third to fifth columns present results computed on successful runs only. Mean overall accumulated size corresponds to the total number of nodes processed in the population when the maximum number of fitness evaluation is reached.

Bloat control method	Successful runs	Mean number of evaluations for success	Mean successful individual size	Mean accumulated size before success	Mean overall accumulated size
Symbolic Regression					
NoLimit	87%	12320	22.1	221634	20203244
DepthLimit	85%	12517	22.0	220897	4902013
$\operatorname{DynLimit}$	93%	14835	18.8	235510	2152695
DynOpEq	74%	50648	21.8	696070	1391389
HARM5	99%	13162	14.8	125011	1081575
HARM40	88%	14991	18.4	280149	3019076
Artificial Ant					
NoLimit	36%	15265	55.2	1058498	38038917
DepthLimit	29%	12103	43.3	671771	13445970
DynLimit	28%	25213	46.6	1373064	7471147
DynOpEq	40%	37368	51.0	3064943	18704826
HARM5	39%	16396	18.3	272691	1615314
HARM40	46%	22278	35.6	816279	4057703
Parity-6					
NoLimit	97%	12607	52.3	896412	26772717
DepthLimit	89%	13127	50.6	698269	8769320
DynLimit	92%	12148	40.3	438914	3954319
DynOpEq	94%	35339	34.1	955259	2853804
HARM5	79%	25728	17.6	369804	1173898
HARM40	96%	16634	29.4	589192	3 137 083

of the same success rate as other methods (similar or better performances), while keeping tight control over accumulated size (less computation).

## Acknowledgements

We acknowledge financial support from NSERC (Canada) and FQRNT (Québec), and access to supercomputing facilities of CLUMEQ/Compute Canada.

## 1. REFERENCES

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Figure 1: HARM-GP source and target histograms.



Figure 2: Size and fitness for the Artificial Ant problem: (top) best fitness median (over the 100 runs) according to the number of fitness evaluations; (middle) mean size median at each generation; and (bottom) best fitness median against accumulated size.